$$\frac{\partial x_{wavg}}{x_{wavg}} = \frac{\partial \left[\sum w_i x_i \right]}{\sum w_i x_i}$$